

# MedeA GIBBS: The Reference Approach for Fluid Properties and Sorption

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## 1 Overview

*MedeA GIBBS* aims at computing equilibrium properties using Monte Carlo molecular simulations. It has the following main features:

- Determination of phase properties. Statistical ensembles: NVT, NPT, semi-grand canonical, osmotic
- Adsorption of fluids in solids through  $\mu$ VT simulations (Grand canonical ensemble), imposing an external field defined on a grid. Among other applications, it allows you to simulate the adsorption of molecules in microporous crystalline solids of cubic or orthorhombic structure.

- Calculation of fluid phase equilibria, either two-phase (L-V, L-L) or multiphase (L-L-V...), using the Gibbs ensemble at imposed pressure or imposed global volume, without an explicit interface, but one separate simulation box per phase.

Unlike molecular dynamics, Monte Carlo methods do not aim at describing system evolution with time. Instead, Monte Carlo methods sample the possible configurations of the system in a way that satisfies the conditions of thermodynamic equilibrium, *on average* provided the structure of molecules and their interaction energy is known (see Section Monte Carlo methods). Consequently, some post-processing features of the GIBBS menu (Continue a Run, Convergence, View configuration(s), View adsorption graphs, Cations location analysis) are specific to this tool while they are not fundamentally different from those of *MedeA LAMMPS*.

*MedeA GIBBS* works on pure fluids as well as multi-component mixtures. The possible types of particles are:

- atoms
- rigid molecules
- fully flexible molecules, either linear, branched or cyclic
- semi-flexible molecules, with a rigid part and a flexible part

The following forms of energy may be accounted for:

- dispersion-repulsion energy (Lennard-Jones or exp-6 centers of force)
- electrostatic energy (partial electrostatic charges)
- stretching, bending, and torsion energy (flexible molecules only).

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**Note:** Polarization energy, the action of the electrostatic field on the force centers, considered as polarizable, is not considered explicitly in most forcefields.

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In a way, similar to many studies of adsorption or phase equilibria, *MedeA GIBBS* is most efficient with *United Atom* forcefields, such as *TraPPE-UA* or *AUA*. In such forcefields the hydrogens are generally lumped onto a heavy atom, for example, a methyl group may be considered as one united-atom.

In the case of rigid molecules, any coordinates can be attributed to dispersion-repulsion centers and electrostatic charges. Any forcefield (*United Atoms* or *All Atoms*) can be used for such molecules. This means that electric charges can be placed outside atomic centers. In small molecules like H<sub>2</sub>, N<sub>2</sub>, O<sub>2</sub>, H<sub>2</sub>S, and H<sub>2</sub>O this allows an excellent representation of molecular interactions.

To simulate efficiently the various statistical ensembles and molecular types, more than 10 types of Monte Carlo moves are available. They use the pre-insertion and rotational bias for rigid molecules, and configurational bias for flexible molecules (see section Statistical Bias Monte Carlo moves).

*MedeA GIBBS* works in batch mode: data files are read in and result files are written out. A single job may comprise several tasks (for instance two tasks for the simulation of adsorption at two fugacity levels). Each simulation is usually decomposed into several runs, which may include different Monte Carlo move probabilities, frequency of result storage, or the number of iterations, all under user control.

- The main average properties are computed and printed in the `Job.out` file of the run.
- For phase equilibria involving more than two components, the average composition of each phase is also determined and printed in `Job.out`.
- In  $\mu$ VT simulations, the heats of adsorption are computed and printed in `Job.out`.
- The GIBBS computations are generally followed by a specific post-processing step. The specific options are thus part of the GIBBS menu:
  - `Gibbs >> Continue a run` (for extending the run if convergence is slow)
  - `Gibbs >> Convergence` (for visualizing convergence of energy versus number of steps)
  - `Gibbs >> View configuration` (view molecules and/or solid in the stored configurations)

- Gibbs >> View adsorption graphs (view adsorption isotherm)
- Gibbs >> Cations location analysis

## 2 Basic Workflow

The purpose of the present section is to introduce the first-time user to the various steps involved in simulations with the *MedeA GIBBS* software, which may be useful as several types of input files are required and several output files are generated in any simulation.

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**Note:** The legacy file `potparam.dat` containing the forcefield parameters used by GIBBS is provided with each release of *MedeA*, but it is no longer updated. You cannot change the name of this file, but you can still edit it, provided you store it in a different folder, e.g. *Forcefields/custom/*.

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**Note:** The units in GIBBS input and output files are as follows:

- Distances (ex. Lennard-Jones diameter, AUA offset) in Å
  - Energy parameters (Lennard-Jones epsilon) are expressed as  $U/k_B$ , i.e. they scale like temperature, and their unit is *K*.
  - Molecular mass in *g/mol*
- 

**Note:** Molecular mass does not influence the course of the Monte Carlo simulation, as it does not influence the potential energy terms. However, it plays an important role in property calculations.

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In the case of united atoms (*Trappe-UA*, *AUA*) the molecular mass attached to the force center includes the mass of constituting atoms (e.g. 12.01 g/mol for C, 13.01 g/mol for CH, 14.02 g/mol for CH<sub>2</sub>).

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**Note:** Hydrogens are not considered explicitly in the course of the simulation, but their positions can be reconstructed from the position of carbons if required.

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### 2.1 Defining Molecular Species

Molecules present in a Monte-Carlo run are defined by `molecule.sci` files. One file per species should be available. A `molecule.sci` file may be created by **File >> New non periodic structure**. Through **File >> Open**, the user may also open an already created molecule file.

Several molecular files used with GIBBS are stored in *MD/Structures/Gibbs* and its subfolders.

Although forcefield assignment is available, it is advised that users use first the molecular files of this folder, if present. This is particularly advised in the case of potential models for small molecules, which contain frequently off-atom Lennard-Jones sites or electrostatic charges. Charges are expressed in multiples of electron charges and distances are in Å.

For instance, the *TIP4P* model of water (file `H2O - TIP4P.sci`) involves one Lennard-Jones site on the oxygen, but no such site on hydrogens. Two positive electrostatic charges are set on the hydrogens, and a negative charge is located at 0.15 Å of the oxygen nucleus, on an *X atom (ghost atom)*.

Another example is the molecule of methane (CH<sub>4</sub>). In the united atom description, a single Lennard-Jones site is used ( $\sigma = 3.7327$  Å,  $\epsilon = 149.92$  K), without electrostatic charges. The molecular mass (16.043 g/mol) refers to one carbon + four hydrogens. Hydrogens are not considered (they appear as blank fields in the “*Forcefield Atom type*” of the spreadsheet of the molecular builder.)

Several formats can be read in *MedeA* (i.e. \*.car, \*.xyz, \*.xmol, .pdb, .mol2), but the assigned forcefield parameters (atom types and charges) can only be saved in the *sci* format.

The global electrostatic charge of a molecule should be neutral, i.e. here:  $0 \pm 10^{-5}e$ .

## 2.2 MedeA GIBBS Flowcharts

By clicking on **Gibbs** >> **Define computation**, a new window appears, where the user can create in just a few steps a complete flowchart where all the simulation parameters and details are set.

In the Materials Design Flowchart:

- **Start** is always set by default as the first stage in the flowchart.
- **Set Variables** brings up an *optional* stage: Here you can define as many control variables as for all following simulation stages (i.e. temperature, pressure, ...).
- **Gibbs: Monte Carlo** brings up the main simulation stage. A new window pops when the user opens this stage. In this stage, the user can create the main *MedeA GIBBS* flowchart.

The *MedeA GIBBS* flowchart should *always* contain the following stages:

- **Start** (default)
- **Initialize**
- One of the main *MedeA GIBBS* stages:
  - **Single-phase properties**
  - **Phase equilibrium**
  - **Adsorption**
- **Run** (at least one run stage needs to exist)

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**Note:** Stages provide access to a bare minimum of options, all other parameters are set to their default values and their values are accessible through **Advanced Settings** in each stage.

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### Start Stage

The first part of any *MedeA GIBBS* flowchart is always the **Start** stage.

### Initialization Stage

Initialization is achieved through the **Initialize Gibbs** stage. This stage sets the parameters for the interatomic potential: the method for dealing with electrostatic charges, the cutoff, and minimum non-bond distance. These parameters control the way that the interactions between the system particles are computed. Default values are proposed by *MedeA GIBBS*, but tests should be made depending on the specific systems to be studied and the suggestions of the developers of the forcefield used.

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**Note:** Zero or negative values for the **cut-off** are interpreted as setting half the box length as cut-off (in case of non-cubic boxes, the smallest box length is selected).

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- **Random seed**
  - *-1* means that a new seed for the random generator is defined for clock time (used if the simulation must be repeated with different parameters)

- 0 means that the standard seed is taken (two successive runs with the same input on the same machine will provide the same results)

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**Note:** *Include intramolecular* electrostatic has no impact on rigid molecules, but can be required for long, flexible molecules with more than one functional group. Of course, this increases the computation time. The use of intramolecular electrostatic (or vdW) interactions depends on the forcefield used.

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After initialization of GIBBS, you chose the type of simulation: **Single Phase Properties**, **Phase Equilibria & Properties** or **Adsorption**.

- **Single phase properties** refers to monophasic fluid simulations in the NPT, NVT, Osmotic, or Semi-grand Canonical ensembles of either pure compounds or mixtures. It allows also the determination of gas solubility constants in the fluid through Widom test insertions.
- **Phase equilibria & Properties** refer to the simulations of phase equilibrium without explicit interface in the Gibbs ensemble (either isochoric or isobaric). *MedeA GIBBS* will then create one simulation box per phase.
- **Adsorption** refers to simulations in the Grand Canonical ensemble ( $\mu$ VT) where fluid molecules interact with a microporous solid.

### Single-phase properties Stage

Depending on the type of simulation chosen, the parameters that refer to the corresponding ensemble must be defined (temperature, pressure, chemical potential, etc.). Also, in this stage, the flowchart defines the `molecule.sci` files (one for each species of the system). There are two possible ways to read in the `molecule.sci` files; if open in *MedeA*, click on **Add component from MedeA**, if the file is saved on the computer, use **Add component from a file**.

*Initial configuration:* in contrast to LAMMPS or VASP, GIBBS does not necessarily require the initial positions of all particles in the NVT or NPT ensembles.

There are currently three (3) choices for the creation of the initial configuration for a *MedeA GIBBS* simulation, as is shown in the *Advanced Settings* mode of any type of *MedeA GIBBS* simulation:

Start this simulation :

1. **by creating the structure** : *MedeA GIBBS* fills the simulation box with the number of molecules that the user has specified (molecules are placed on a regular lattice with random orientations)
2. **from a previous structure** : *MedeA GIBBS* gets the simulation box(es) from a previous simulation
3. **from a built system** : *MedeA GIBBS* imports the entire system from *MedeA* or from a saved `sci` file (available for single phase simulations only)

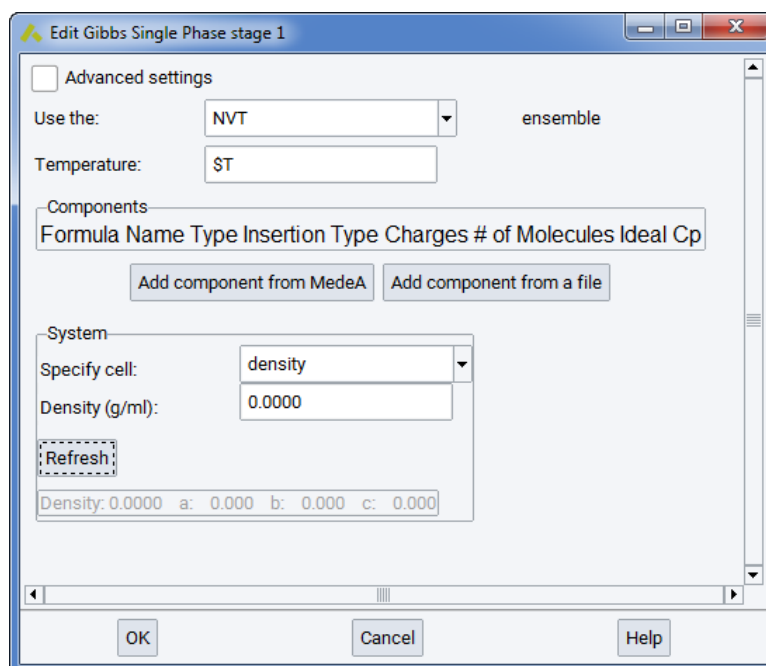
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**Note:** When starting the simulation **by creating the structure**, you can avoid problematic overlap of molecules in dense phases (such as a liquid phase in the NPT ensemble) by starting at a low density (typically 20 to 60% of the expected final density) and check that the intermolecular attraction is sufficient to allow the simulation box to shrink.

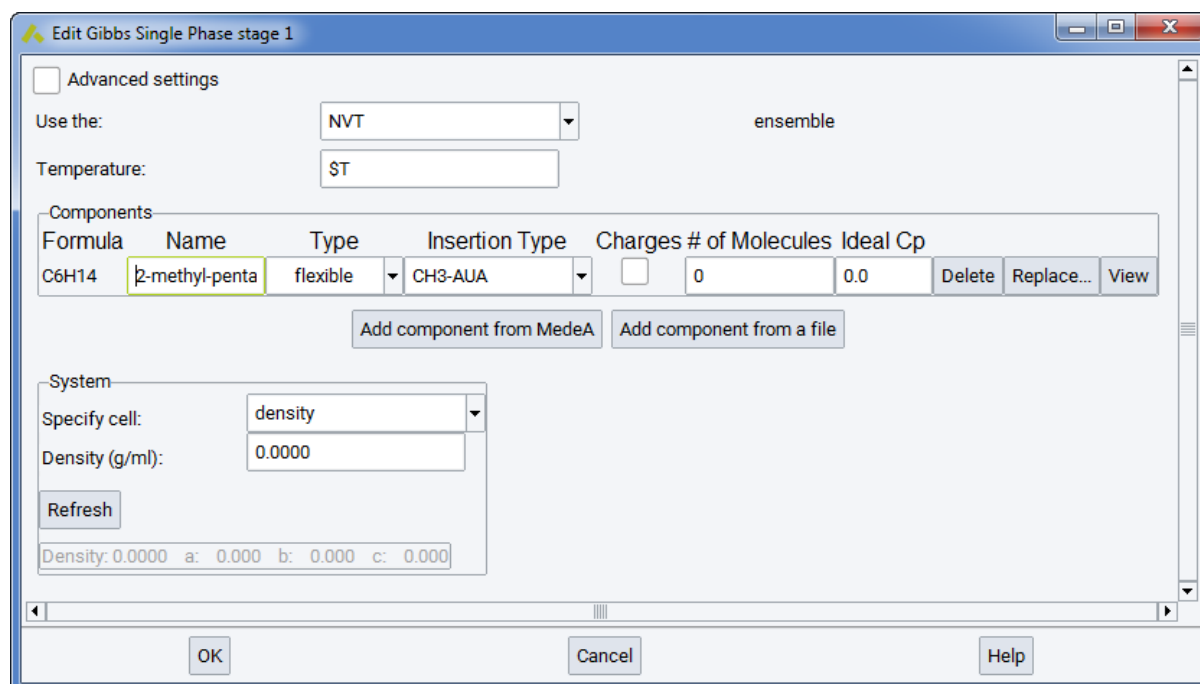
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### Simulation of a Monophasic Fluid in the NVT or NPT Ensemble

**Single Phase Properties** offers NVT and NPT ensembles: In these ensembles, only input files listed at the beginning of this section are required. The rest of the necessary input files, to start the simulation, are created automatically when the user fills in the corresponding fields in the simulation flowchart.



**Note:**  $\$T$  refers here to the variable  $T$  entered for Temperature in the **Set Variables** stage of the flowchart. Similarly,  $\$P$  refers to the variable  $P$  for Pressure.



In the *Components* section, you can define different components and their occurrences. When a new component is added from *MedeA* or from a file, it appears as a new line in the frame. The column *Name* refers to the identification of this component by *MedeA*. The column *Type* refers to the molecular structure (*flexible*, *rigid*, or *semi-flexible*). This refers to different ways of defining molecular structure in *MedeA GIBBS* and depends on definition of the molecular model used (see section [Defining molecular species](#))

When calculating a solubility constant for a given molecule, the molecular type of the solute should be entered in the list, and test insertions should be explicitly added with a reasonable frequency in the *MC moves* section of the **Run** stage.

The *Insertion type* refers to the force center that is used to test positions of the solute in the pre-insertion

bias. The diameter of this force center should not be larger than the smallest dimension of the molecule. The `Insertion type` field is filled by a default value in *MedeA* for a given molecule.

The column *charges* informs the user of partial electrostatic charges in the molecules he has selected. Expert users may decide to neglect electrostatic charges for either molecule, but this is not advised in the general case.

The column *ideal cp* refers to the ideal heat capacity of the pure component considered, at the temperature considered, in J/mol/K. This input is needed when thermodynamic properties are computed from fluctuations (see section Thermodynamic derivative properties for more details). However, it does not influence the course of the simulation, as it is used at the post-processing stage only.

In the *Components* section, you can define the system size and shape in a number of different ways. More specifically:

`Specify cell` provides a variety of options for controlling the size of the initial configuration of the system. Thus, for example, choosing `Specify cell density` will produce cubic cells in which the cell edges are determined based on the overall composition and density. Similarly, choosing `Specify cell density,c` will create tetragonal cells based on the density and specified c dimension, while choosing `Specify cell a,b,c` creates orthorhombic cells using the a, b and c lengths provided (in which case the density cannot be specified independently since it is fixed by the composition).

The full set of options for `Specify cell...` is as follows:

- `Density` : Density is provided in units of g/mL and can be either a numeric value or a previously defined variable (e.g.  $\$d$ ).
- `density,a` Density is provided in units of g/mL and can be either a numeric value or a previously defined variable (e.g.  $\$d$ ). The side of the simulation box (a) is provided in units of Å and can only be numeric values.
- `density,b` Density is provided in units of g/mL and can be either a numeric value or a previously defined variable (e.g.  $\$d$ ). The side of the simulation box (b) is provided in units of Å and can only be numeric values.
- `density,c` Density is provided in units of g/mL and can be either a numeric value or a previously defined variable (e.g.  $\$d$ ). The side of the simulation box (c) is provided in units of Å and can only be numeric values.
- `density,a,b` Density is provided in units of g/mL and can be either a numeric value or a previously defined variable (e.g.  $\$d$ ). The sides of the simulation box (a and b) are provided in units of Å and can only be numeric values.
- `density,a,c` Density is provided in units of g/mL and can be either a numeric value or a previously defined variable (e.g.  $\$d$ ). The sides of the simulation box (a and c) are provided in units of Å and can only be numeric values.
- `density,b,c` Density is provided in units of g/mL and can be either a numeric value or a previously defined variable (e.g.  $\$d$ ). The sides of the simulation box (b and c) are provided in units of Å and can only be numeric values.
- `a,b,c` The sides of the simulation box (a, b, c) are provided in units of Å and can only be numeric values.
- `volume` : The volume of the simulation box is provided in units of Å<sup>3</sup> and can only be a numeric value.
- `a,b,c,alpha,beta,gamma` The angles of the simulation box ( $\alpha$ ,  $\beta$ ,  $\gamma$ ) are provided in units of degrees and can only be numeric values.

Once the flowchart is created, the user may run the simulation. At first, a series of consistency checks on the input data is performed and related messages are written in the `gibbs.log` output file. If the consistency tests are successful, the code proceeds by writing several types of result files.

First types of result files are history files, the main of which are `Aavg1.res` `Aavg2.res`... These files contain instantaneous values of energy, volume or pressure taken at specific times during the Monte Carlo simulation. `Ajt1.res` contains the observed fluctuations and allows computing thermodynamic derivative properties like thermal expansivity based on these fluctuations.

The code is also writing two types of files: the configuration file (`conf1.res`) and the restart files (`restart-odd.res` and `restart-even.res`) which provides a snapshot of the last system configuration. Other files, characterized with extension `.mol` (as `Aconf1.mol`) allow visualizing a snapshot of the molecules in the last configuration. *MedeA*'s post-processing utility reads the content of `Aavg1.res` files to compute average volume, density or pressure, together with the estimated statistical uncertainties.

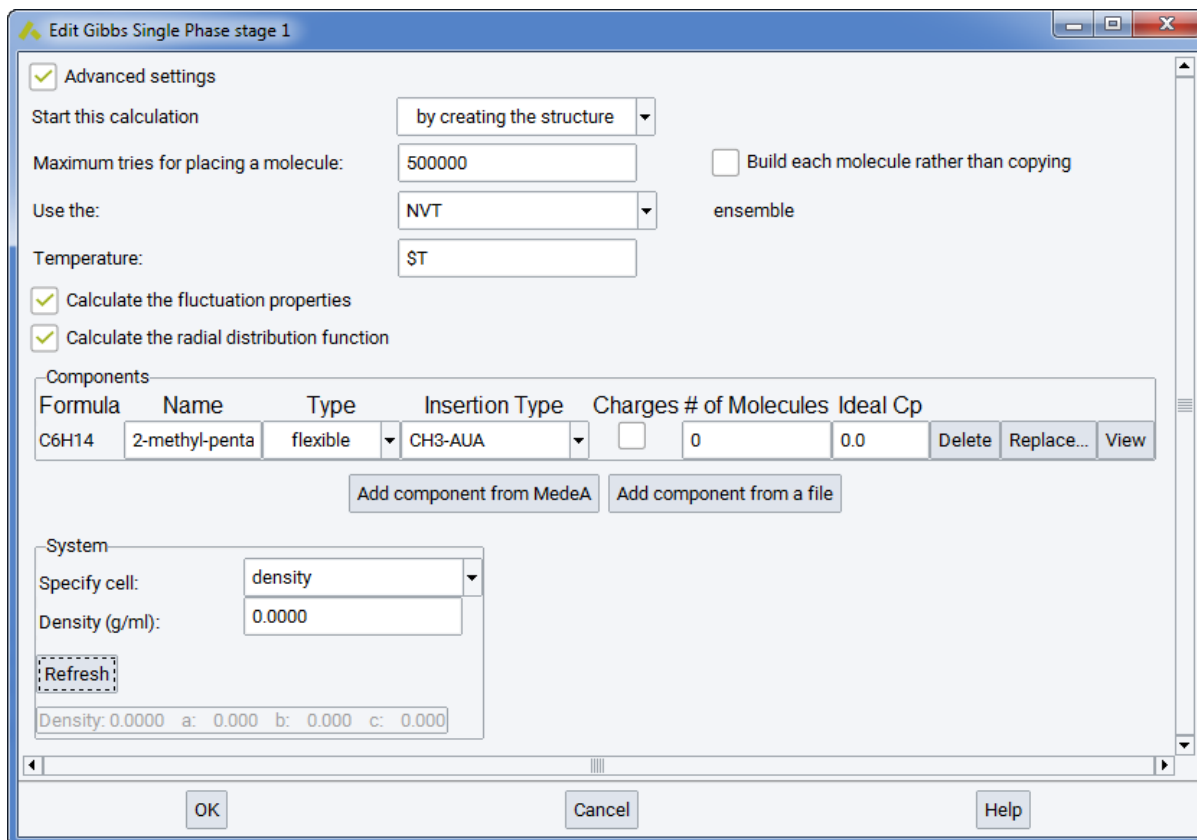
### Advanced Settings

**Start this calculation** : the way of creating the initial configuration for the simulation. There are currently three available options:

- **by creating the structure** : *MedeA GIBBS* creates the initial configuration to be used in the simulations, by placing each molecule of each species in a simulation box of the specified dimensions and at the specified density
- **from a previous structure** : *MedeA GIBBS* takes the configuration from a previous run (`conf<x>.dat` file should be present at the previous job's directory, on the job server)
- **from a built system** : *MedeA GIBBS* reads the configuration created by *MedeA* builders (e.g. *Amorphous Materials Builder*) or other tools, or a structure generated by another simulation run (e.g. a *MedeA LAMMPS* simulation), or any other system that can be opened in *MedeA*. Introduction of the pre-built system in the *MedeA GIBBS* stage is done through the two buttons present in the *Components* section of the GUI:
  - Add system from MedeA , or
  - Add system from a file

**Maximum tries for placing a molecule** : maximum number of orientations tested for building the initial box with the requested number of molecules (this is corresponding to parameter `indexmax_initconf`, in the `control.dat` GIBBS input file). This parameter is defined if **Start this calculation** is set to **by creating the structure** (default).





Advanced settings

Start this calculation:

Maximum tries for placing a molecule: 
 Build each molecule rather than copying

Use the:  ensemble

Temperature:

Calculate the fluctuation properties

Calculate the radial distribution function

Formula	Name	Type	Insertion Type	Charges	# of Molecules	Ideal Cp			
C6H14	2-methyl-penta	flexible	CH3-AUA		0	0.0	Delete	Replace...	View

System

Specify cell:

Density (g/ml):

Density: 0.0000 a: 0.000 b: 0.000 c: 0.000

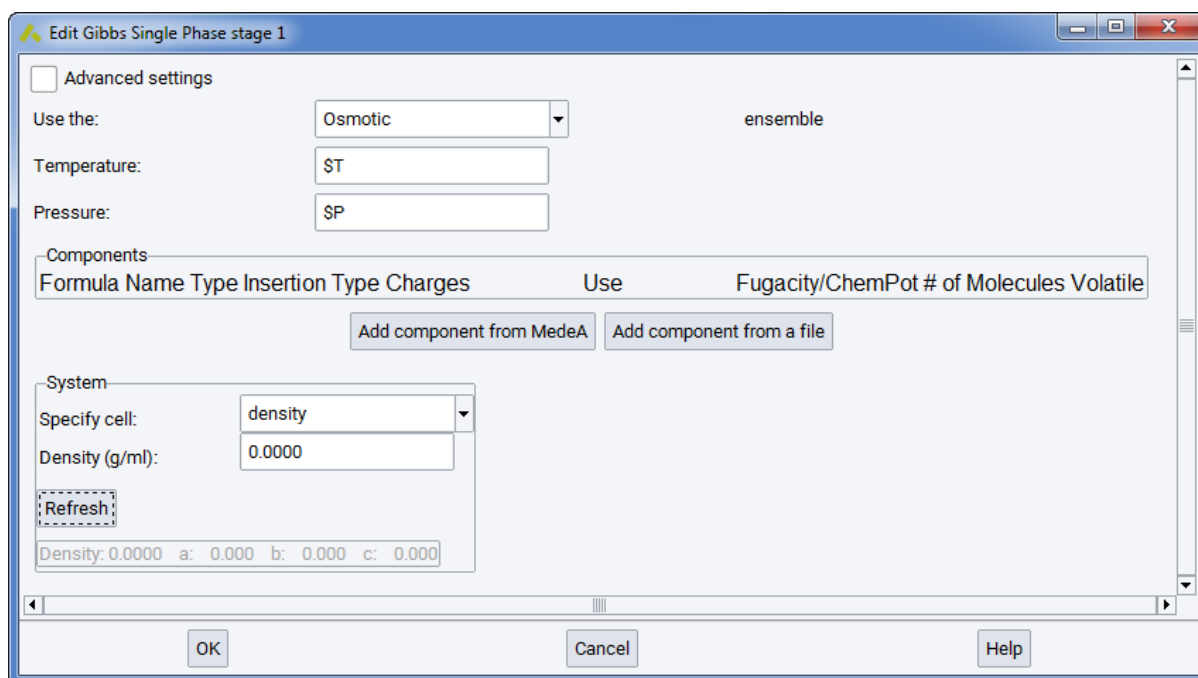
**Build each molecule rather than copying** : checking this box means that the random number generator will generate new molecular conformations for each molecule when building the initial box with the requested number of molecules.

Two optional boxes may be checked to generate more analysis: **Calculate the fluctuation properties** (i.e. thermodynamic derivative properties, see section Thermodynamic derivative properties) and **Calculate the radial distribution function**, a standard way to characterize the structure of liquids.

## Simulation of a Monophasic Fluid in the Osmotic Ensemble

The osmotic ensemble is a way to simulate phase equilibria of fluids with solids (e.g. polymeric materials) without simulating the fluid phase. There may be any number of molecular types for the fluid and the solid. The aim is the computation of solubility of fluid components in solids under specific stress conditions and fluid pressures. It should be noted that stress may differ from fluid pressure. The osmotic ensemble may also be used to compute fluid phase equilibria involving a heavy component that cannot enter the light phase, for instance an equilibrium between a gas and a heavy alkane under pressure. In this case, the stress variable in the osmotic ensemble simulation must be identical to the pressure in the preliminary NPT simulation of the light phase.

**Single Phase Properties** offers access to the Osmotic ensemble. In this ensemble, only input files listed in the beginning of this section are required. The rest of the necessary input files, in order to start the simulation, are created automatically when the user fills in the corresponding fields in the simulation flowchart. Alternatively, the simulation can begin from the resulting configuration of a past simulation (e.g. from a resulting configuration of a previous NPT compression of a heavy compound, with zero or very small inclusion of a light compound).



**Note:**  $\$T$  refers here to the variable  $T$ , entered for Temperature in the **Set Variables** stage of the flowchart. Similarly,  $\$P$  refers to the variable  $P$  for the total stress entered again in **Set Variables** stage of the flowchart.

In the *Components* section, you can define different components and their occurrences. When a new component is added from *MedeA* or from a file, it appears as a new line in the frame.

- The column **Name** refers to the identification of this component by *MedeA*. The column **Type** refers to the molecular structure (flexible, rigid, or semi-flexible).
- The column **Insertion type** refers to the force center that is used to test positions of the solute in the pre-insertion bias. The diameter of this force center should not be larger than the smallest dimension of the molecule. The *Insertion type* is chosen by *MedeA*.
- The column **Charges** informs the user of partial electrostatic charges in the molecules he has selected. Expert users might decide to neglect electrostatic charges for a molecule, but this is not advised in the general case.
- The column **Fugacity/ChemPot** refers to the imposed fugacity or chemical potential (respectively) of each component, as in the Grand Canonical and semi-grand canonical ensemble simulations. Before a simulation is made in this ensemble, the user should determine the chemical potentials of the fugacities in the fluid phase by an NPT simulation involving Widom test insertions. As the fugacity (or the chemical potential) plays the same role in this ensemble as in GCMC simulations, it is mandatory to use insertion and deletion moves in the Run stage(s).
- The column **Volatility** refers to the identification of the volatile component(s) in the system, i.e. the compounds of which the total number in the system may vary (these should always have a total charge equal to zero), and the non-volatile (i.e. the heavy compounds of which the total number in the system will remain constant throughout the simulation). Consequently, the *Volatility* column will control the way the insertion/deletion move weights are selected, for on the components of the system.

Once the flowchart is created, the user may run the simulation. At first, a series of consistency checks on the input data is performed and related messages are written in the `gibbs.log` output file. If the consistency tests are successful, the code proceeds by writing several types of result files.

The first type of results files are simulation history files, the main of which are `Aavg1.res` `Aavg2.res` .... These files contain instantaneous values of energy, volume or pressure taken at specific times during the Monte Carlo simulation.

The code is also writing two types of output files: the configuration file (`conf1.res`) and the restart files (`restart-odd.res` and `restart-odd.res`) which provides a snapshot of the last system configuration. Other files, characterized with extension `.mol` (as `Aconf1.mol`) allows visualizing a snapshot of the molecules in the last configuration. *MedeA*'s post-processing utility reads the content of `Aavg1.res` files to compute average volume, density, or pressure, together with the estimated statistical uncertainties.

### Advanced settings

**Start this calculation** : the way of creating the initial configuration for the simulation. There are currently three available options:

- **by creating the structure** : *MedeA GIBBS* creates the initial configuration to be used in the simulations, by placing each molecule of each species in a simulation box of the specified dimensions and at the specified density
- **from a previous structure** : *MedeA GIBBS* takes the configuration from a previous run (`conf<x>.dat` file should be present at the previous job's directory, on the job server)
- **from a built system** : *MedeA GIBBS* reads the configuration created by *MedeA* builders (e.g. *Amorphous Materials Builder*) or other tools, or a structure generated by another simulation run (e.g. a *MedeA LAMMPS* simulation), or any other system that can be opened in *MedeA*. Introduction of the pre-built system in the *MedeA GIBBS* stage is done through the two buttons present in the *Components* section of the GUI:
  - **Add system from MedeA** , or
  - **Add system from a file**

**Maximum tries for placing a molecule** : maximum number of orientations tested for building the initial box with the requested number of molecules (this is corresponding to parameter `indexmax.initconf`, in the `control.dat` GIBBS input file). This parameter is defined if **Start this calculation** is set to **by creating the structure** (default).

**Build each molecule rather than copying** : checking this box means that the random number generator will generate new molecular conformations for each molecule when building the initial box with the requested number of molecules. This parameter is defined if **Start this calculation** is set to **by creating the structure** (default).

Two optional boxes may be checked to generate more analysis: **Calculate the fluctuation properties** (i.e. thermodynamic derivative properties, see section Thermodynamic derivative properties) and **Calculate the radial distribution function** , a standard way to characterize the structure of liquids.

## Phase equilibrium Stage

Depending on the type of simulation chosen, the parameters that refer to the corresponding ensemble must be set (temperature, pressure, chemical potential, etc.). Also, in this stage, the flowchart defines the `molecule.sci` files (one for each species of the system). There are two possible ways to read in the `molecule.sci` files; if open in *MedeA*, click on **Add component from MedeA** , if the file is saved on the computer, use **Add component from a file** .

*Initial configuration*: in contrast to LAMMPS or VASP, GIBBS does not necessarily require the initial positions of all particles in the Gibbs ensemble.

There are currently two (2) choices for the creation of the initial configuration for a *MedeA GIBBS* simulation, as is shown in the *Advanced Settings* mode of any type of *MedeA GIBBS* simulation:

**Start this simulation** :

1. **by creating the structure** : *MedeA GIBBS* fills the simulation box with the number of molecules that the user has specified (molecules are placed on a regular lattice with random orientations)
2. **from a previous structure** : *MedeA GIBBS* gets the simulation box(es) from a previous simulation

## Simulation of Fluid Phase Equilibria in the Gibbs Ensemble

A Gibbs ensemble simulation requires the same input files (molecular structure files) as the monophasic NVT or NPT simulations considered above. The specification of the number of phases in the **Gibbs** >> **Phase Equilibria & Properties** flowchart stage is sufficient to ask e.g. a two-phase simulation.

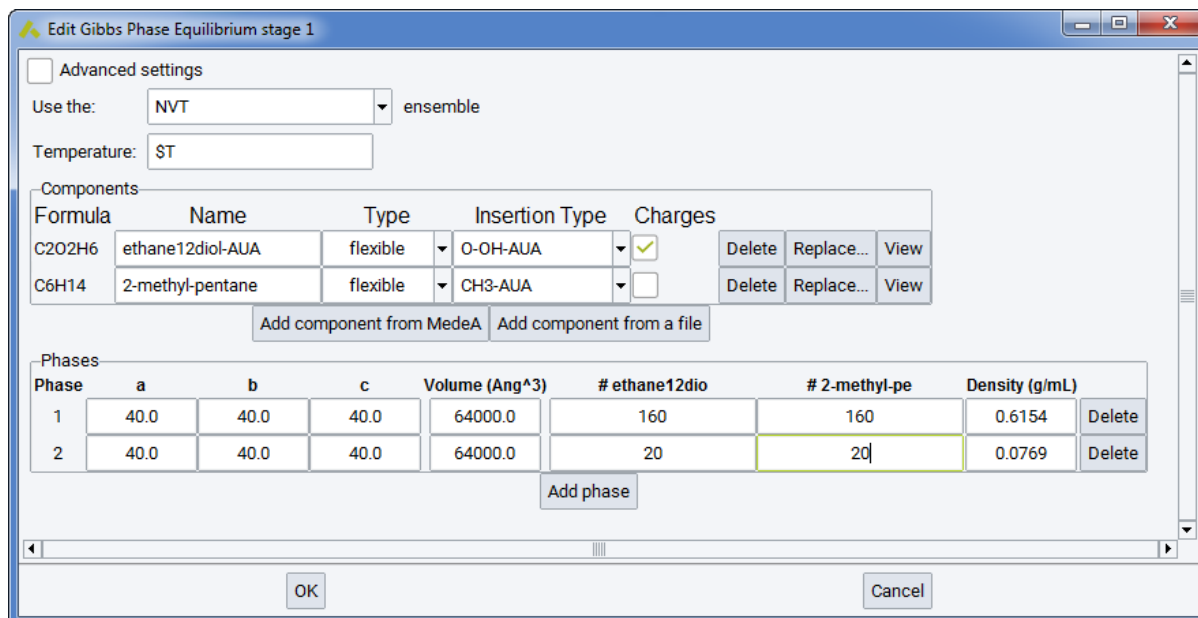
This means that two simulation boxes with different densities will be considered for two-phase equilibria, three simulation boxes for three-phases. Each box must be representative of the phase considered, i.e. it should be homogeneous (as the interface is not explicitly modeled) and should contain at least 2-3 molecules of each type.

Among the practical differences between phase equilibrium and monophasic simulations, the following are most important:

- provide the initial number of molecules in each box (columns “# molecule1”, “#molecule2”, etc.)
- provide the initial size (columns a, b and c, in Å) for each simulation box (or the initial density in g/cm<sup>3</sup>)
- allocate a significant frequency to Monte Carlo transfer moves AND to volume change moves in the definition of the Run stages
- You cannot apply the Gibbs ensemble NPT to the phase equilibrium of a single component, as this would not respect the phase rule. This is possible only in the NVT ensemble when the sum of the phase volumes is imposed.

These selections can be quite sensitive and critical for the successful convergence of your phase equilibrium calculations. For instance, the phase densities and compositions of a binary system will tend toward the same values in both boxes if the average composition of the systems falls in the monophasic domain in the P, x diagram. To converge toward different properties in the vapor and liquid boxes, the composition should be well inside the liquid-vapor coexistence domain.

A Gibbs ensemble simulation at imposed volume or imposed pressure is made automatically when there is more than one phase. As specific differences between phase equilibrium and monophasic simulations, you must allocate a significant frequency to transfer Monte Carlo moves, and provide the initial number of molecules and box size for each simulation box. These selections can be quite sensitive and critical for successful calculations.



Phase	a	b	c	Volume (Ang^3)	# ethane12dio	# 2-methyl-pe	Density (g/mL)	
1	40.0	40.0	40.0	64000.0	160	160	0.6154	Delete
2	40.0	40.0	40.0	64000.0	20	20	0.0769	Delete

The output files are qualitatively the same as in monophasic fluid simulations, except that all those of a single simulation box are duplicated. Thus result files are `Aavg1.res`, `Aconf1.mol`, ... for the first fluid phase and `Bavg1.res`, `Bconf1.mol`, ... for the second fluid phase. As the chemical potential is a byproduct of Gibbs ensemble simulations, the chemical potentials in both boxes are gathered in the `Cp1.res` file.

Pressure equilibrium is reached if there is a significant overlap of the error bars of the virial pressure in all phases that are in equilibrium. Chemical equilibrium is reached when a significant number of Monte Carlo transfer moves have been accepted for each molecular type. These statistics are available in the `final1.res` file for run 1, `final2.res` for run 2, etc.

For simulations of phase equilibrium at imposed volume, post-processing provides the coexisting densities and the virial pressure in each phase (see section Thermodynamic integration for fluid phase equilibria). Usually, the uncertainty of the virial pressure is significantly larger in the liquid phase (several bars). Then the vapor phase pressure is a more reliable estimation of the equilibrium pressure.

For simulations at imposed pressure  $P$ , it should be checked that the virial pressure of each phase is in agreement with  $P$  (i.e., that the error bar on virial pressure contains  $P$ ).

In simulations of a binary mixture at imposed pressure, the equilibrium mole fractions and densities are also printed in the `Job.out` file.

### Advanced Settings

Advanced settings:

Start this calculation by creating the structure ▾

Maximum tries for placing a molecule:   Build each molecule rather than copying

Use the: NVT ▾ ensemble

Temperature:

Calculate the fluctuation properties  Calculate the radial distribution function

### Adsorption Stage

Depending on the type of simulation chosen and the corresponding statistical ensemble used, certain parameters must be defined. For sorption simulations in the GCMC ensemble these parameters are temperature, pressure, and chemical potential.

Also, in this stage, the flowchart includes the `molecule.sci` files (one for each species of the system). There are two possible ways to read in the `molecule.sci` files; if open in *MedeA*, click on `Add component from MedeA`, if the file is saved on the computer, use `Add component from a file`.

*Initial configuration*: in contrast to LAMMPS or VASP, GIBBS does not necessarily require the initial positions of all particles in the GC ensemble.

There are currently two (2) choices for the creation of the initial configuration for a *MedeA GIBBS* simulation, as is shown in the *Advanced Settings* mode of any type of *MedeA GIBBS* simulation:

Start this simulation :

1. `by creating the structure` : *MedeA GIBBS* fills the simulation box with the number of molecules that the user has specified (molecules are placed on a regular lattice with random orientations)
2. `from a previous structure` : *MedeA GIBBS* gets the simulation box(es) from a previous simulation

### Simulation of Adsorption in the Grand Canonical Ensemble

Compared with the above-mentioned simulations of fluid phases, the simulation of adsorption in microporous solids differs due to the use of the Grand Canonical ensemble and the treatment of the solid as an external forcefield. However, the way of defining the components of the system are identical to bulk fluid phases.

A Grand Canonical simulation is characterized by setting `Gibbs >> Adsorption` in the flowchart and by specifying the chemical potential of each molecular species, since this is an imposed parameter in this ensemble. Alternatively, the user may enter fugacity, which is equivalent to partial pressure at low pressure,

instead of chemical potential (see sections Forcefields for materials simulations and Evaluation of the Chemical Potential by Test Insertions). In *MedeA GIBBS*, the unit for chemical potential is Kelvin (as it is expressed in  $\mu/k_B$ ). Fugacities may be entered as mPa, Pa, kPa, bar, atm.

The treatment of the solid is by far the most characteristic feature of the simulation of adsorption. Indeed, it is a common procedure to consider the solid as rigid, and this allows reducing considerably computer time through a preliminary computation of the interaction energy between the guest molecules and the microporous solid.

For this purpose, you must provide a unit cell of the solid (section **Solid for Adsorption** in the **Gibbs Adsorption stage**) such as it can be obtained from crystal databases of *InfoMaticA*.

---

**Note:** *MedeA GIBBS* will consider the unit cell as P1 symmetry and requires an assigned forcefield type and charge for each atom of the unit cell, according to the forcefield used.

---

The preliminary computation of interaction energies is made by *MedeA GIBBS* before starting the Monte Carlo iterations. It makes use of the solid coordinates file together with a specific parameter set as input and generates different energy grid files. These grid files are named this way because they contain the potential energy on the nodes of a grid with regular spacing in x, y, z covering the unit crystal cell. The default grid spacing is 0.2 Å.

---

### Grid file size

For a typical box size of 25x25x25 Å, it implies the calculation and storage of 125<sup>3</sup> energy values, i.e. more than 2.5 million points. Such files are commonly more than 100 MB, and they may cause memory problems if spacings lower than 0.2 Å are considered. Therefore, you can select **Delete grid file**, which deletes the grid files after usage in the current job, from the **Advanced settings** options.

---

The solid unit cell should be selected as small as possible because the simulation box can contain multiple unit cells. Various grid files can be generated depending on the type of potential energy to be considered:

- the dispersion-repulsion energy grid file (generally one such file per force center of the adsorbed molecules),
- the electrostatic energy grid file (a unique file corresponding to the interaction of a unit point charge with the solid).

Using a simulation box larger than the unit cell is possible through the parameters *na*, *nb* and *nc* of the panel (integer values). The resulting length of the simulation box along a, b and c directions is provided. You create a small model and assign forcefield parameters (or calculate the grid with VASP), and then use a larger cell, containing *na x nb x nc* cells.

The functional form of the zeolite-guest energy potential may be either Lennard-Jones or Buckingham (i.e. exponential repulsion and 1/*r*<sup>6</sup> dispersion). Once the grid files are generated, they may serve to simulate the adsorption in the system considered by running *MedeA GIBBS* simulation at various conditions of temperature and chemical potential, for pure components and mixtures as well. Making the grid files precedes the actual Monte Carlo simulation.

**VASPtGIBBS** : generation of the electrostatic grid by VASP

The format of the electrostatic grid makes it possible to use a *locpot* file generated by a VASP single point analysis. Although it is not strictly required that VASP is used to optimize the solid structure, it is recommended (the electrostatic field would be erroneous if the atom nuclei do not occupy stable positions). It is, of course, recommended that a small unit cell be selected to minimize VASP computing time and to use multiple unit cells to have a representative number of adsorbed molecules if needed.

---

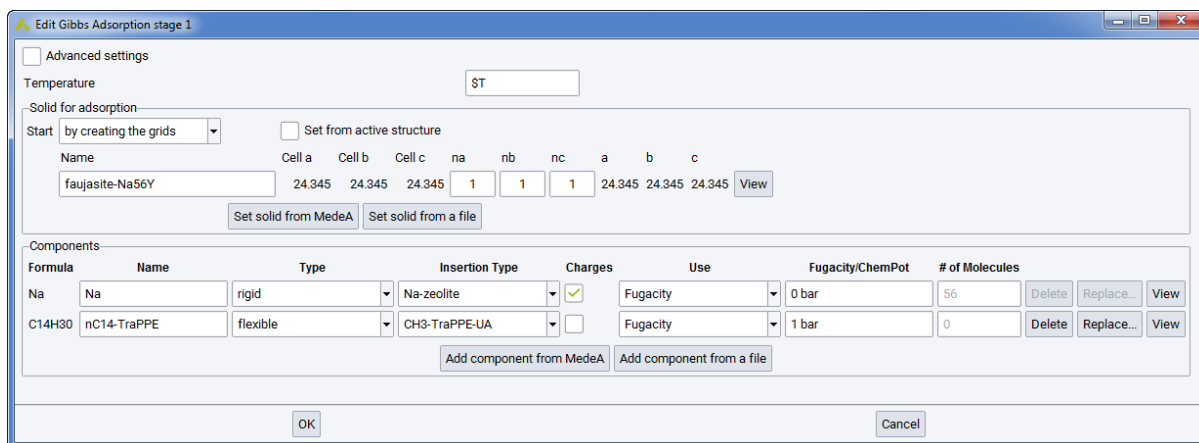
**Note:** Be careful that the dispersion-repulsion grid is still needed when the *locpot* file from VASP is used.

---

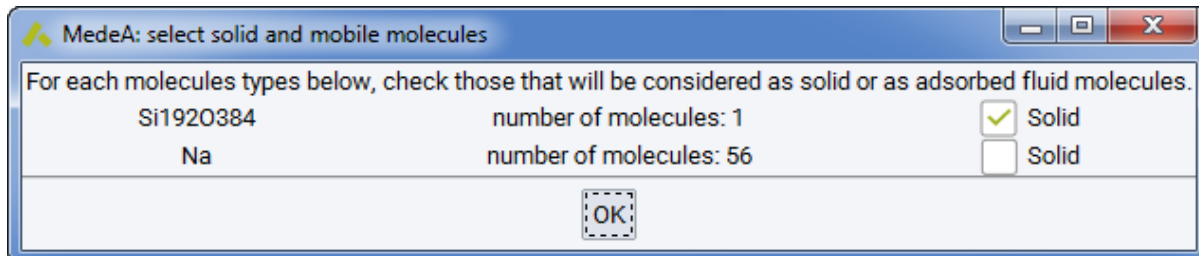
Grand Canonical ensemble simulations involve specific moves, namely insertions and deletions of molecules, which should be attempted often enough (their frequencies are allocated by *MedeA GIBBS* and are typically

0.30). You can select other frequencies than proposed by *MedeA*, but enforce with **Normalize** that the sum of *Move probabilities* is equal to 1. The weight of the different molecules in each Monte Carlo move may be changed if the acceptance rate is low for a specific molecular type.

The output files generated by *MedeA GIBBS* are similar to bulk fluid simulations: *Aavg1.res* files provide the history of the number of molecules and energy with the progress of the Monte Carlo simulation, *Aconf1.mol* allows a graphic display of adsorbed molecule with rasmol, etc. Post-processing is also presenting a lot of common features with bulk fluid simulations in the NPT or NVT ensembles. The averages are provided in the file *Job.out*, particularly the average number of molecules as well as the evaluation of the isosteric heat of adsorption.



In some cases, it may be useful to perform a Grand Canonical simulation of adsorption in a system that contains a rigid framework and guest molecules (for instance a faujasite zeolite and water molecules). Then, *MedeA* lists the identified solids or molecules, and asks you to select the adsorbates in the component stage below:



### Advanced Settings



### Run Stage

The final part of the simulation is one or more *Run* stages. Here the number of total steps for the simulation run, the intervals for writing (in the corresponding output files) the configuration, the main averages, the

restart file, etc are defined. Also, the various move probabilities are defined. Depending on the ensemble in which the simulation takes place, different types of Monte Carlo moves are available:

- *Internal moves:*
  1. *regrowth* of a molecule (flexible and semi-flexible molecules, all ensembles), based on configurational bias
  2. *internal rotation* of one atom in a chain (around the axis of its immediate neighbors)
  3. *pivot* (rotation of a part of the molecule around an axis crossing a center, branched and semi-flexible molecules, all ensembles)
  4. *reptation* (linear flexible and semi-flexible molecules, all ensembles), including configurational bias
  5. *concerted rotation* (linear flexible and semi-flexible molecules, all ensembles)
  6. *double bridging* (linear flexible and semi-flexible molecules, all ensembles)
  7. *internal double rebridging* (linear flexible and semi-flexible molecules, all ensembles)
  8. *stretching move* (atomic translation)
- *Rigid moves:*
  1. *rigid body translation* of a molecule (all molecular types, all ensembles),
  2. *rigid translation and rotation* (displacement move, displacement of a molecule by moving it to a random position and orientation in the same box)
  3. *rigid body rotation* of a molecule (all molecular types, all ensembles)
  4. **exchange** of two molecules,
  5. *swap* of two molecules of different types
- *Transfer moves:*
  1. molecular *transfers* between phases (Gibbs ensemble)
  2. *insertions and deletions* (Grand Canonical ensemble), also Widom test insertions
- *Volume changes*

Depending on the type of molecules (i.e. flexible or rigid) certain types of moves may bring up error messages when set to non-zero values. Some examples are provided in the FAQ section.

---

**Note:** Averages must be calculated for a system which has been well equilibrated, i.e. when long term averages of energy fluctuations (as well as other property fluctuations) do not show significant drift.

---



---

**Note:** You do not need to set any of the move probabilities by hand. *MedeA* assigns automatically default values and weights on the types of moves that are relevant to the molecules present in your simulation and their specific structure(s), as well as the type of simulation (the statistical ensemble).

---

Subsequent **Run** stages may be used to have an equilibration run, followed by a production run. Each **Run** stage, after the first one, will use as an initial configuration the last configuration of the previous **Run** stage.

## 2.3 Adsorption Isotherms

The **Adsorption isotherm** stage consists in automating the simulation of several state points in the Grand Canonical ensemble at different values of chemical potential or fugacity. Its purpose is two-fold:

- avoid that the user spends unnecessary time in launching several different Adsorption jobs to compare with experimental sorption isotherms,



- organize the computations in such a way that the final stage of a simulation may be used to initialize the next point, allowing thus to simulate adsorption (increasing fugacities) and desorption (decreasing fugacities).

Creating the Adsorption isotherm stage is justified by their frequent occurrence in expressing adsorption data on microporous solids, either for characterizing their pore structure (BET analysis is based on nitrogen sorption isotherm at 77K) or their performance in adsorbing specific compounds.

It is also important to identify possible hysteresis effects (i.e. different paths on adsorption and desorption) and optimizing sampling efficiency.

**Edit stage: Gibbs Adsorption Isotherm**

Temperature:       Fugacities  
 Range :   
 Units :  ▼

Initialize by previous step     Add desorption path

---

This is an adsorption isotherm job at 300 K

The adsorption solid is not yet defined

There are currently no selected adsorbate.  
 Edit the adsorption stage to select one or more.

Gibbs calculations be will started one after another,  
 and the final configuration of a run will be used as initial in the next.

The **Gibbs Adsorption Isotherm** stage, allows you to see the important parameters at one glance: *Temperature*, the *fugacity values*, as well as the choices of *initializing by previous step*, and also running a *desorption* path.

Clicking on the button **Adsorption Flowchart** brings up a pre-compiled *MedeA GIBBS* flowchart.

- The stage **Initialize** is where the calculation of interactions is tuned (setting of Ewald parameters, cut-off, functional forms of Nonbond Forcefield terms). The defaults are set depending on the forcefield that is read in *MedeA*.
- The stage **Adsorption** is where the adsorbent (solid) and the adsorbates (components) are defined, as well as the number of unit cells, and the grid spacing.

---

**Note:** Adsorbed components are often called Adsorbates, while the solid is termed Adsorbent. It is a good practice to define molecules with meaningful names.

---

- The first **Run** stage is where the details of the equilibrium run are defined, such as the number of Monte Carlo steps, Monte Carlo move frequencies, and printing details for the result files.
- The second \* **Run** stage is where the details of the production run are defined, such as the number of Monte Carlo steps, Monte Carlo move frequencies, and printing details for the result files.

After defining the *solid* and all *components*, you will see a summary of Adsorption Isotherm conditions, e.g.:

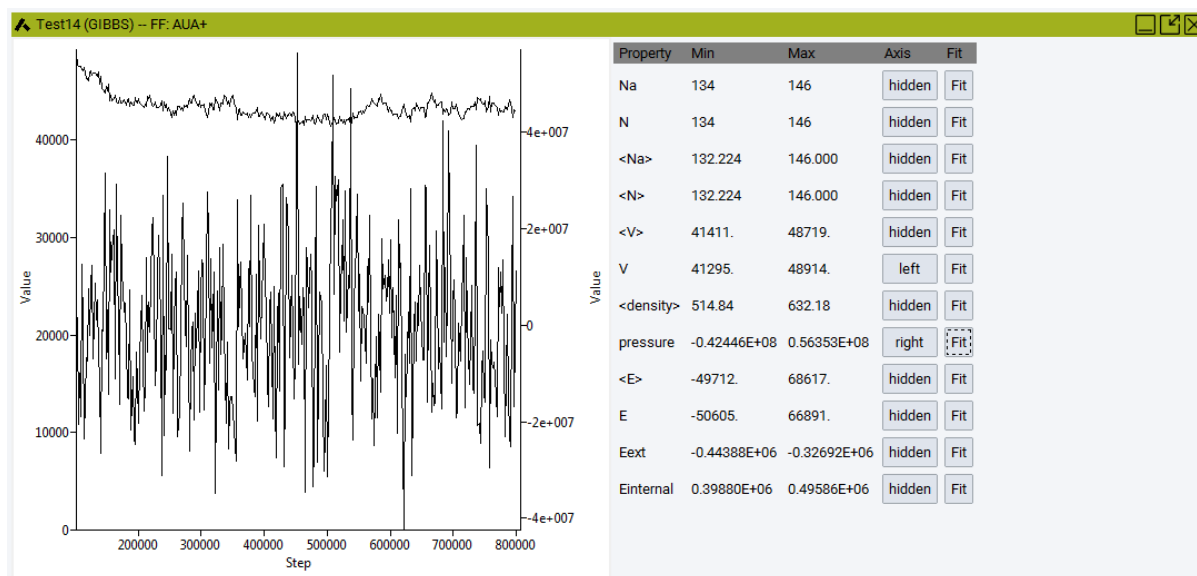
This is an adsorption isotherm job at 298K.  
 The grid will be created from the solid \\* (C)88 (P1) ~CNT-(11,0)-semiconductor  
 Current adsorbate is: methane-Moeller  
 Gibbs calculations will be started independently,  
 And can run in parallel according to TaskServer availability.

### 3 Launching and Analyzing Gibbs Computations

**Define computation** : This opens a flowchart editing panel and allows you to define the type of computation together with specific settings for each sampling run. Add a title to your computational job and submit with **Run** to the JobServer. Depending on your configuration, *MedeA GIBBS* runs efficiently on multiple processors with shared memory, thus speeding up your simulations. Depending on system size and architecture, this is very efficient with 4 to 16 cores.

**Continue a run** : Allows extending a computation based on the final configuration. A set of Monte Carlo steps are added to the ones defined in the original flowchart and the simulation run is extended accordingly.

**Convergence** : Allows to monitor properties and their computed averages over the duration of the Monte Carlo simulation, e.g.: Number of molecules A Na, overall number of molecules, N , Volume V, density, pressure, and energies.

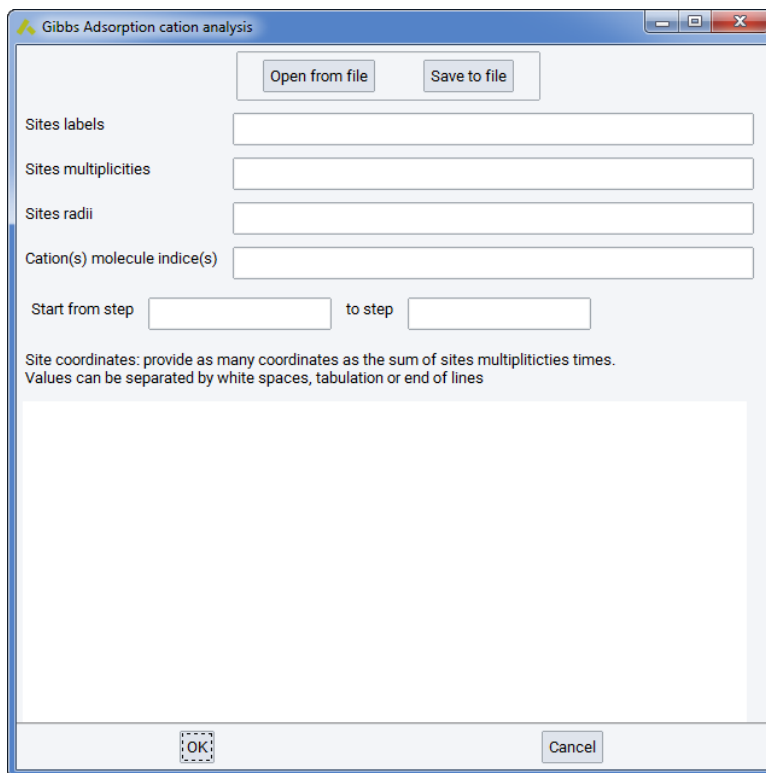


#### View configuration(s) :

While analyzing configurations from adsorption computations, you will be asked, “Merge configuration with adsorption solid?” to display the solid in addition to the adsorbate. You can use the combined system as the input structure for diffusion studies in LAMMPS.

**View adsorption graphs** : After an adsorption isotherm job has been completed (Gibbs: Adsorption Isotherm), you can view the sorption graphs and the isosteric heat of sorption as a function of fugacity.

**Cations location analysis** : Cation location analysis can be performed in systems where cations have been allowed to move throughout the simulation, i.e. they were not considered part of the solid but part of the fluid, with zero insertion/deletion moves but non-zero translation moves. You will be prompted with a small wizard where you will need to specify the positions (sites) that you want to search for the existence of cations throughout the simulation or during a certain part of it. A `confs<x>.res` needs to be present in the simulation, to be analyzed. This file will exist if you have specified that average configurations are kept during the simulation run.



## 4 Results

The result filenames are written in the respective task directory and consist of a name and an extension:

- `.mol`: visualization files
- `.pdb`: visualization files
- `.res`: files containing, at successive timesteps, the value of several physical quantities

In general, the filenames are like `<Phase><Name><run>.<extension>`, as explained below.

`<Phase>` is an uppercase letter corresponding to the simulation box: A for the first phase, B for the second, and so on.

`<Name>` describes the file contents: avg corresponds to the average values of various physical quantities at successive timesteps.

`<run>` is the number of the run during which the file was generated.

`Bavg<run>.res` contains the average quantities for the third run and the second phase of the system.

### 4.1 GIBBS simulation results files

#### Used Forcefield Parameters File

The `potparam.res` file contains all the forcefield parameters, which are used in the current simulation. This file is written by default in each task directory.

#### Main Average Files

The names of these files are: `Aavg<run>.res`, `Bavg<run>.res`, `Aavg<run>.res`, `Bavg<run>.res` etc. The number at the end of the filename refers to the run number and the letter at the beginning of the filename refers to the corresponding phase.

These files contain the instantaneous values and the averages (computed in intervals) of various physical quantities. The length of these intervals (number of steps in between two averages recordings) is defined in each `Run` stage of the flowchart, in the *Intervals* tab, by the *Writing the main averages* option.

The energies in the `.res` files are given as  $\epsilon/k_B$  (as are the energy dispersion-repulsion parameters of the `potparam.dat` forcefield file) and therefore in temperature units, K.

---

**Note:** This file contains only potential energies; as kinetic energy is not part of a Monte Carlo simulation.

---

Average quantities recorded in this file are taken from the last interval, current quantities are taken from the last step. There are 19 columns in this file:

- step number,
- current number of type 1 molecules for this phase,
- current number of molecules for this phase,
- average number of type 1 molecules for this phase,
- average number of molecules for this phase,
- average total energy, including the long distance correction (K),
- average electrostatic energy, including the grid-molecule electrostatic energy (K),
- average grid-molecule energy: dispersion-repulsion and electrostatic (K),
- average electrostatic grid-molecule energy (K),
- current total energy, without the long distance correction (K),
- current total intramolecular energy, without the long distance correction (K),
- current induction energy (K), (*not implemented*)
- current intramolecular energy (K),
- average volume of the phase ( $\text{\AA}^3$ )
- current volume of the phase ( $\text{\AA}^3$ )
- average density of the phase ( $\text{kg/m}^3$ )
- current pressure (Pa) (requires `Calculate the pressure with the virial formula`)
- current dipole moment (*requires induction computation - not implemented*)
- current energy due to the external field (in K) (*requires external electric field - not implemented*)
- These files are used to visualize the evolution of these quantities. They are also used to compute the averages on a whole simulation, according to the convergence criteria, and printed at the `Job.out` file present in the job directory.

### Composition Files (`Acom<run>.res`)

These files, with names such as `Acom<run>.res`, contain the molar fractions of each constituent. They are useful only for a system with three or more constituents. For a system with up to two constituents, the `Aavg<run>.res` file suffices for the determination of the phase composition.

### Configuration Files (`conf<run>.res`)

There is one such file for each run (with names such as `conf<run>.res...`). They contain the information needed to restart a simulation from the last configuration of a previous run.

### Run summary files (`final<run>.res`)

There is one such file for each run (with names such as `final<run>.res`). For each type of possible moves, they contain the total number of attempts and successes.

---

**Note:** A summary of the attempted and performed moves, in each run and each phase, is also provided in `Job.out` in the task directory.

---

### Chemical potential files (`Cp<run>.res`)

These files contain averages collected at regular intervals for each run (with names such as `Cp<run>.res`), if phase equilibrium is simulated. Each line contains the current step number and the chemical potential for each constituent in each phase.

These properties are not obtained by simple ensemble averages. The long term average is determined with specific statistical rules in *MedeA GIBBS* and reported in `Job.out`.

### Visualization files (`Aconf<run>.mol`)

These files, with names such as `Aconf<run>.mol`, are written by default for each run (the number at the end of the filename refers to the number of the run).

### Fluctuation files (`Ajt<run>.res`, `Ajt<run>.res`)

These files contain averages collected at regular intervals for each run if the `Calculate the fluctuation properties` checkbox is checked in the Gibbs stage (in a `Single Phase Properties`, or a `Phase Equilibria & Properties`, or an `Adsorption` simulation run). They are used to compute derived properties such as the Joule-Thomson coefficient.

---

**Note:** Derivation of the Joule-Thomson coefficient, isentropic compressibility, and total heat capacity requires that the ideal  $C_{p, id}$ , which cannot be computed by Monte Carlo simulations and therefore should be provided for each component of the system in the Gibbs Stage.

These properties are not obtained by simple ensemble averages. The long term average is determined with specific statistical rules in *MedeA GIBBS* and reported in `Job.out`.

---

### Radial Distribution Files (`Agder<run>.res`, `Agder.elec<run>.res`)

These files, with names such as `Agder<run>.res`, `Agder.elec<run>.res`, contain the radial distribution function  $g$ , calculated during the simulation run between all centers of forces in the `Agder1.res` file, or between all electrostatic centers in the `Agder.elec<run>.res` file. The partial  $g(r)$  are calculated at the same intervals as the intervals in which the main averages are recorded. These files are written only if the `Calculate the radial distribution function` checkbox is checked in the Gibbs stage (in a `Single Phase Properties`, or a `Phase Equilibria & Properties`, or an `Adsorption` simulation run).

### Simulation continuation files

#### Restart file (`restart.dat`)

The restart file contains, in binary form, the full simulation state at a given moment.

## 4.2 MedeA GIBBS results (calculated properties)

### Job.out

The simulation summary and the computed properties are all reported in the `Job.out` file that is present in the top directory a given Job. Computed properties are reported as computed in the converged part of the entire simulations. If the run remains unconverged or seems to be poorly converged, appropriate information is printed to aid the user in continuing the simulation or redefining the input parameters and resubmitting the Job.

### Isosteric Heat of Adsorption (in Job.out)

The Isosteric Heat of Adsorption and the Grid Isosteric Heat of Adsorption (Isosteric heat of adsorption at low coverage) are printed in the results part of `Job.out`, after the simulation has finished.

### Adsorption Isotherm Summary (in Job.out)

When performing an Adsorption Isotherm simulation, one or more tables are printed in the end of the `Job.out` file, summarizing the simulation results over the entire range of fugacities.

In the case of an adsorption isotherm calculation of a single species, the table columns are:

- Iteration
- Fugacity (input data)
- Amount sorbed (number of molecules per simulation box)
- Amount sorbed (mol of sorbed compound per kg of solid)
- Isosteric Heat of Adsorption

In the case of an adsorption isotherm calculation of more than one species, several tables are printed. The first table is a general summary of the calculation, with the following columns:

- Iteration
- Amount sorbed (total number of molecules per simulation box)
- Amount sorbed (mol of all sorbed compounds per kg of solid)
- Isosteric Heat of Adsorption

The second table printed (in the case of an adsorption isotherm calculation of more than one species) has  $n+1$  columns, where  $n$  is the number of different sorbed species:

- Iteration
- Fugacity of species 1
- Fugacity of species 2
- Fugacity of species  $n$

Then next table printed (one per sorbed species,  $i$ ) with two columns:

- Fugacity of species  $i$
- Amount sorbed (molecules of species  $i$  per simulation box or mol of sorbed species per kg of solid)

And finally, a table is printed (one per sorbed species,  $i$ ) with two columns:

- Fugacity of species  $i$
- Molar fraction (of species  $i$ )

## 5 MedeA GIBBS Variables for Computed Properties

In *MedeA GIBBS*, computed properties follow a common naming scheme.

To distinguish between the different stages, the run number is appended:

```
property_calc_{run number}
```

If the property depends also on the molecular species or/and phase (simulation box), the number corresponding to the species is appended and the letter of the simulation box is appended as well, so the general name scheme is:

```
property_calc_{phase}_{run}
```

or

```
property_calc_{species}_{phase}_{run}
```

---

**Note:** Phases are named using consecutive letters (i.e. A, B and C for the first, second and third phase respectively) and runs are named using consecutive numbers (i.e. 1, 2 and 3 for the first, second and third run respectively).

---

You can add computed properties to tables, for example when performing a set of calculations with varying temperatures.